Automated Configuration of MIP solvers

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- Decisions that are left open during algorithm design
 - numerical parameters (e.g., real-valued thresholds)
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Prominent parameters in MIP solvers

- Preprocessing
- Which type of cuts to apply
- MIP strategy parameters
- Details of underlying linear (or quadratic) programming solver

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 - Perform manual optimization in 76-dimensional space
 - Complex, unintuitive interactions between parameters
 - Humans are not good at that
- CPLEX automated tuning tool (since version 11)
 - Saves valuable human time
 - Improves performance

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This paper: application study for MIP solvers

- Use existing algorithm configuration tool (PARAMILS)
- ► Use different MIP solvers (CPLEX, GUROBI, LPSOLVE)
- Use six different MIP benchmark sets
- Optimize different objectives (runtime to optimality/MIP gap)

- 1. Related work
- 2. Details about this study
- 3. Results
- 4. Conclusions

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Parameter Optimization Tools and Applications

- COMPOSER [Gratch & Dejong, '92; Gratch and Chien, '96]
 - Spacecraft communication scheduling
- CALIBRA [Diaz and Laguna, '06]
 - Optimized various metaheuristics
- ► F-RACE [Birattari et al., '04-present]
 - Iterated Local Search and Ant Colony Optimization
- ► PARAMILS [Hutter et al, '07-present]
 - SAT (tree & local search), time-tabling, protein folding, ...

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- STOP [Baz, Hunsaker, Brooks & Gosavi, '07 (Tech report)] [Baz, Hunsaker & Prokopyev, Comput Optim Appl, '09]
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 [Baz, Hunsaker & Prokopyev, Comput Optim Appl, '09]
 - Optimized MIP solvers, including CPLEX
 - We only found this work ≈ 1 month ago
 - Main problem: only optimized performance for single instances
 - Only used small subset of 10 $\rm CPLEX$ parameters

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Start with some parameter configuration

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Modify a single parameter

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 $\label{eq:PARAMILS} PARAMILS \mbox{ [Hutter et al., AAAI'07 & '09]:} \\ \mbox{Iterated local search: biased random walk over local optima}$

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 - typically outperforms $\operatorname{BasicILS}$
 - used in this study

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- Results
 - Provably never hurts
 - Sometimes substantial speedups

[Hutter et al., JAIR'09]

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Segmentation faults & wrong results

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 — Local search avoids problematic parameter configurations
- ► Concise bug reports ~→ helped to fix 2 bugs in GUROBI (!)

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Split benchmarks 50:50 into training and test sets

- Optimized parameters on the training set
- Reported performance on the test set
- Necessary to check for over-tuning

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Compare test performance of:

- PARAMILS's configuration $\hat{\theta^*}$
- Default algorithm settings
- CPLEX tuning tool
 - GUROBI and $\operatorname{LPSOLVE:}$ no tuning tool available

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LPSOLVE on WDP instances (150x)

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 - GUROBI 1.1x to 2.2x

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MIP solvers can be configured automatically

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 - http://www.cs.ubc.ca/labs/beta/Projects/ParamILS/
 - off-the-shelf tool (knows nothing about MIP or MIP solvers!)
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- Representative instance set
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- CPU time (here: 10 × 2 days per domain)

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- Use that model to quantify
 - + Importance of each parameter
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 - + Interaction of parameters and instance characteristics
- Per-instance approaches for heterogeneous benchmarks
 - Given a new unseen instance:
 - + Compute instance characteristics (fast)
 - $+\,$ Use parameter config. predicted to be best for the instance

Thanks to:

- Providers of instance benchmark sets
 - Louis-Martin Rousseau
 - Bistra Dilkina
 - Berkeley Computational Optimization Lab
- Commercial MIP solvers for free full academic license
 - IBM (CPLEX)
 - Gurobi
- LPSOLVE developers for their solver
- Compute clusters
 - Westgrid
 - CFI-funded arrow cluster
- Funding agencies
 - Postdoc fellowship from CBIE
 - MITACS
 - NSERC

Backup slides

Baz et al optimized for single instances

"In practice, users would typically be tuning for a family of related instances rather than for an individual instance"

Generalization to sets of instances is nontrivial

- Cannot afford to run all instances for each configuration

 $\rightsquigarrow~FocuseDILS$ adapts # runs per configuration

Further differences

- ▶ Baz et al used older CPLEX version (9.0)
 - defaults improved in newer CPLEX versions
- ▶ Baz et al considered (only) 10 CPLEX parameters
 - and also not all possible values for each parameter
 - in order to improve $\operatorname{Stop}\nolimits\textsc{'s}$ performance
 - → requires domain knowledge

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